

# Pre-Lecture Lesson

## Glossary

Here are some terms we may encounter in our talk:

- **Transmissibility:** how easy it is for a disease to pass from one person to another
- **Susceptibility:** how susceptible (or easily) a person can be infected
- **Exponential growth:** a sequence that grows more as time goes on and gets bigger rapidly. It is dependent on how big the exponent is. For example
  - o  $1^2 = 1, 2^2 = 4, 4^2 = 16, 16^2 = 256, \dots$
  - o  $1^3 = 1, 2^3 = 8, 8^3 = 512, 512^3 = 134,217,728$
  - o  $1^4 = 1, 2^4 = 16, 16^4 = 65,536, 65,536^4 = 1.8 \times 10^{19}$  or 180,000,000,000,000,000,000

And here are some concepts we may encounter:

- The symbol  $\frac{dx}{dt}$  means whatever the change in 'x' is over the change in 't' (which is time). The 'd' means change in.

## Sequences

A sequence is a list of numbers that are in a special order. They follow a specific pattern from one number to the next.

Can you find the pattern in these sequences?<sup>1</sup>

3, 5, 7, 9, ... (the dots mean the list continues forever – to infinity)

5, 10, 15, 20, ...

7, 11, 15, 19, 23, ...

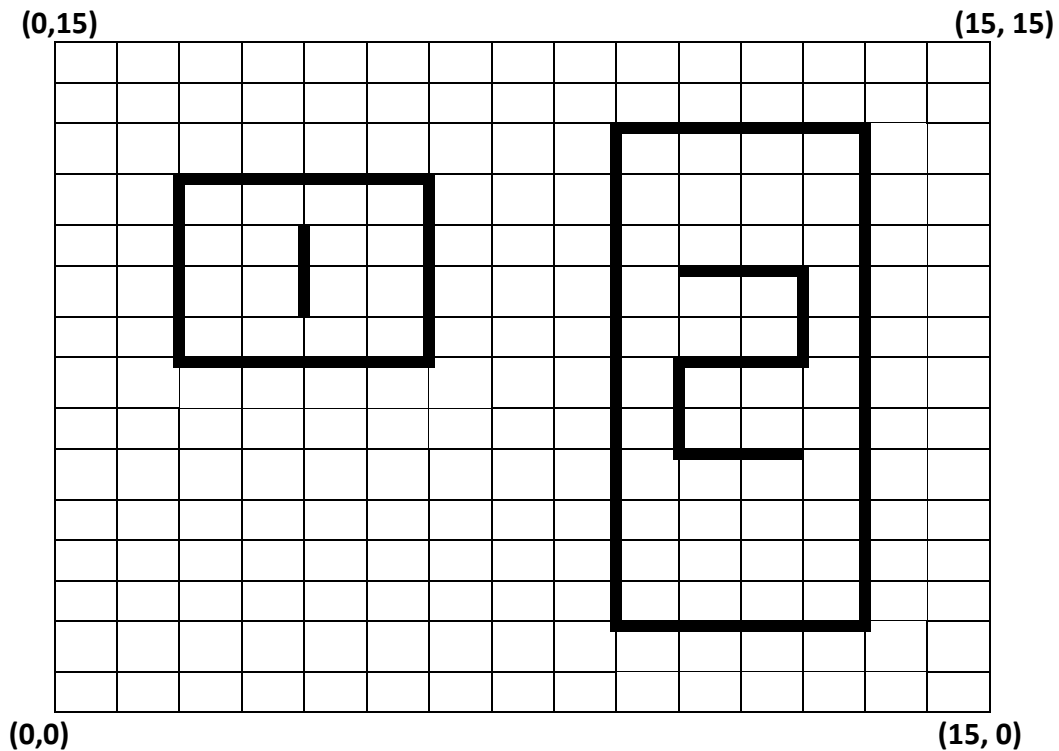
3, 11, 35, 107, ... (this one involves more than one operation)

4, 16, 256, 65536, 4294967296, ...

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<sup>1</sup> **Answer:** first sequence starts at 3 and goes up by 2 each new number; second sequence starts at 5 and goes up by 5 each new number; third sequence starts at 7 and goes up by 4 each time; the fourth sequence starts at 3 and each new number is the number before multiplied by 3 with 2 added to it ( $3 * 3 = 9 + 2 = 11$  ;  $11 * 3 = 33 + 2 = 35$  ;  $35 * 3 = 105 + 2 = 107, \dots$ ). The final sequence is an exponential growth starting at 4,  $4^2 = 16$  ;  $16^2 = 256$  ;  $256^2 = 65,536$  ;  $65,536^2 = 4,294,967,296, \dots$

## Distances on a Graph



What are the coordinates of the square (1) and the rectangle (2)?<sup>2</sup>

Now what is the distance between the upper left corner of the square (1) and the lower right corner of the rectangle (2)?<sup>3</sup>

If you've learned the Pythagorean theorem you can use the coordinates of the points and the following formula:

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

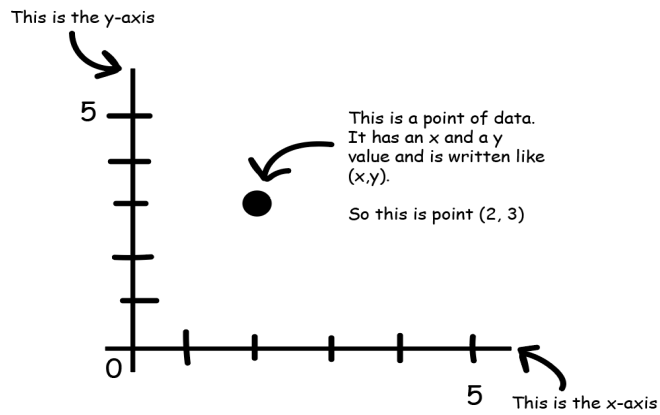
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<sup>2</sup> The square has its 4 corners at (2, 8), (2, 12), (6, 8) and (6, 12). The rectangle at (9, 2), (9, 13), (13, 2), and (13, 13)

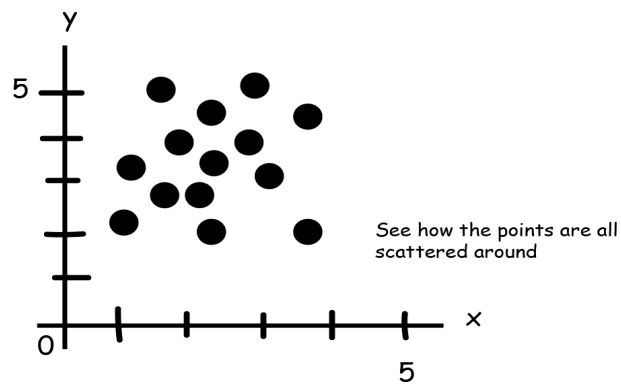
<sup>3</sup> Using the formula, we have points (2, 12) and (13, 2), so  $x_1 = 2$ ,  $x_2 = 13$ ,  $y_1 = 12$ , and  $y_2 = 2$

$$\sqrt{(13 - 2)^2 + (2 - 12)^2} = \sqrt{11^2 + (-10)^2} = \sqrt{121 + 100} = 14.87$$

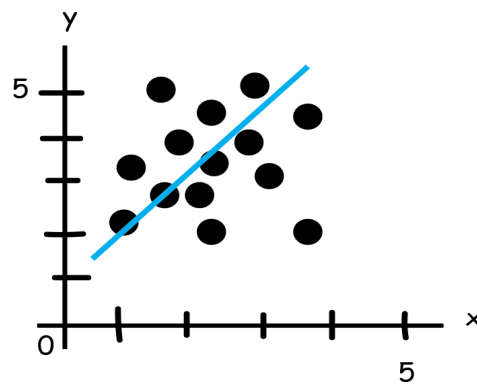
## Scatterplots and Lines of Best Fit



And this is a scatterplot graph:



A line of best fit is a line that is the closest to the most points it can be on the graph. It might go through some points but not others.



This is the equation for a line:

$$y = mx + c$$

Where:

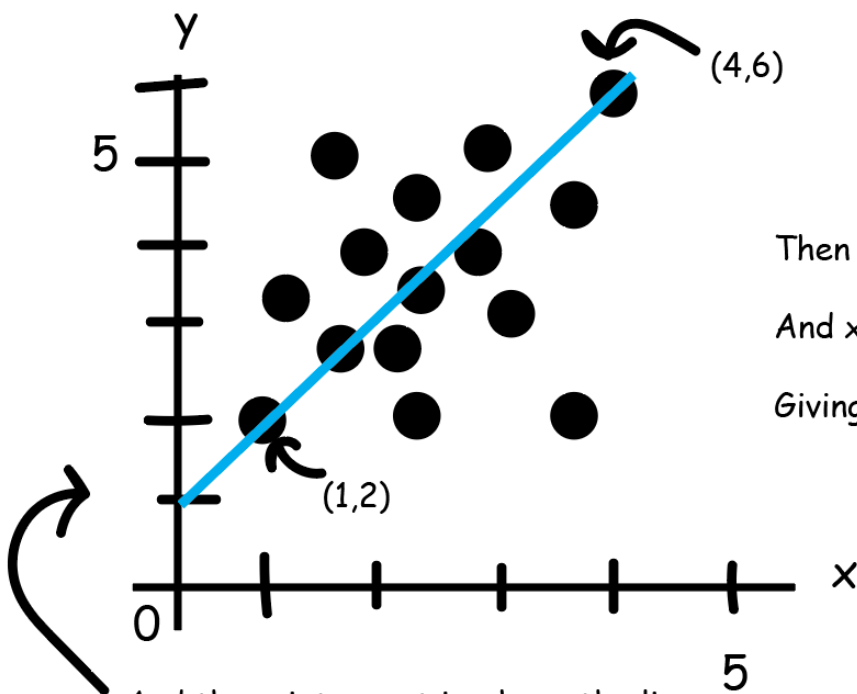
- $y$  is the thing you are looking for (the output)
- $x$  is the thing you are using (the input)
- $m$  is the slope (see below)
- $c$  is the  $y$ -intercept (where the line meets the  $y$ -axis)

Slope formula:

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

And here's how you find it...

First you pick two points on the line.  
We'll use  $(4,6)$  and  $(1,2)$



Then  $y_2 - y_1$  is  $6 - 2 = 4$

And  $x_2 - x_1$  is  $4 - 1 = 3$

Giving slope  $(m) = 4/3 = 1.3$

And the  $y$ -intercept is where the line meets the  $y$ -axis.

Here it's at  $y = 1$ .